

Diffusion in models of active Brownian particles of relevance in biological self-propelled motion

Ernesto M. Nicola* and Benjamin Lindner

*Department Biological Physics,
Max Planck Institute for the Physics of Complex Systems,
Noethnitzer Str. 38,
D-01187 Dresden, Germany*

Self-propelled motion is one of the most fascinating aspects of biological systems. This motion can appear in many different biological contexts either inside cells¹ (*e.g.* molecular motor proteins²) or on the multi-cellular level¹. Simple phenomenological models can help to understand the dynamics of self-propelled entities and their statistics (including their transport properties).

One class of models successfully studied during the last 15 years are active Brownian particles³ (ABP). Here we study, both theoretically and numerically, the effective diffusion coefficient of one-dimensional ABP models. We show that, depending on the choice of the friction function, the diffusion coefficient does or does not attain a minimum as a function of noise intensity. We furthermore discuss the case of an additional bias breaking the left-right symmetry of the system. We show that this bias induces a drift and that it generally reduces the diffusion

coefficient. For a finite range of values of the bias, the models can exhibit a maximum in the diffusion coefficient vs. noise intensity⁴.

Finally, we establish a connection between our results for simple one-dimensional ABP models with detailed models of molecular motors². This link allows us to make experimentally testable predictions about transport properties of molecular motors.

* nicola@pks.mpg.de

¹ D. Bray. *Cell Movements*, Garland, New York, NY, 2001.

² J. Howard. *Mechanics of Motor Proteins and the Cytoskeleton*, Sinauer Associates, Sunderland, Mass., 2001.

³ W. Ebeling, Nonlinear Brownian motion, *Condensed Matter Physics*, 7:539, 2004.

⁴ B. Lindner and E.M. Nicola, *Diffusion in models of biased active Brownian motion*, Eur. Phys. J. (in print, 2008).